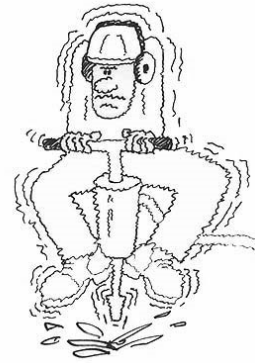


# 機械振動學課程

## Introduction and Overview



Prof. Kuo-Shen Chen  
Department of Mechanical Engineering  
National Cheng-Kung University  
Feb. 14 and 17, 2023

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[www.CartoonStock.com](http://www.CartoonStock.com)



Doc, yesterday someone stole my cell phone, and  
now I feel this phantom vibration alert!

2

## 任課老師介紹: 陳國聲教授

### ■ Education

- BS. Power Mechanical Engineering
  - National Tsing-Hua University
- Ph.D. Mechanical Engineering
  - Massachusetts Institute of Technology (MIT)

### ■ Specialty

- Vibration control, precision machine design, structural analysis, MEMS, nanomechanics, machine tool monitoring & diagnosis

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## Vibration Related Faculty at NCKU ME

### ■ Prof. S. Y. Lee (李森墉教授)

- Ph.D. State University of New York at Buffalo (1984)
- Vibration, applied mathematics, creative design

### ■ Prof. L. W. Chen (陳聯文教授)

- Ph.D. Rensselaer Polytechnic Institute (RPI) (1980)
- Elastic stability, photonic crystals

### ■ Prof. C. H. Liu (劉至行教授)

- Ph.D., Georgia Institute of Technology (2009)
- Topology optimization, structural dynamics, robotics

### ■ Prof. C. J. Lan (陳重德教授)

- Ph.D., NCKU ME (2003)
- FEA, Fracture Mechanics, Energy Harvesting

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## 基本資料

- 選修年級: 3, 4
- 學分: 3
- 上課時間:
  - 週二(7,8) 15:10 – 17:00; 週五 (8) 16:10-17:00.
- 上課地點: 91204
  - 助教: 楊博丞, 張珈銘 RM 91A07
  - 分機 62272

## 基本資料

- 課程網站: Moodle? And <http://klab.me.ncku.edu.tw/>
- Facebook: klab course
- 先修科目
  - 應用力學 (II) (動力學)

## 評分標準

- 作業: 約 8次, total 25 Pts
- Quiz : 三次, ~ 25 pts each
- Possible Term project: 10 Pts
- Total 110 Points

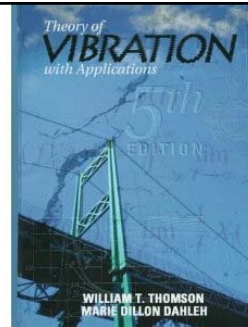


## Possible Term Project (~2人/組)

- To be announced later
- Probably a modal testing project

## Books

- Thomson and Dahleh, Theory of Vibration with Applications, 5<sup>th</sup> Ed. Prentice-Hall



- S. Rao, Mechanical Vibrations, Pearson



## Motivation *The Millennium Bridge a Recent Vibration Problem* (2000-1)



## Modeling and Degrees of Freedom



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## Outline of the Entire Course (I)

- Single Degree of Freedom System
  - Mass-spring systems; mass-spring-damper systems, natural frequencies
  - Free and forced responses
  - Frequency-responses
  - Resonance
  - Shock and vibration isolations
  - Case studies

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## Outline of the Entire Course (II)

- Multiple Degrees of Freedom Systems
  - Normal mode analysis
  - Natural frequencies and mode shapes
  - Vibration absorber
  - Modeling techniques
  - Introduction to finite element method
  - Case studies

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## Outline of the Entire Course (III)

- Continuous Vibrations
  - Modeling of cable, bar, and shaft
  - Solution scheme
  - Modes and natural frequencies
  - Modeling of beam
  - Engineering examples
  - Case studies

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## Outline of the Entire Course (IV)

- Experimental Vibration
  - General procedure
  - Vibration test instruments
  - Modal testing theory
  - Failure diagnostics
  - Case studies

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## Outline of the Entire Course (V)

- Integrated Topics (簡介)
  - Vibration control
    - Feedback control
    - Passive vibration control
    - Active vibration control
    - Noise issues
    - Case studies
  - Advanced vibration topics (簡介)
    - Nonlinear Vibration
    - Random Vibration
    - Rotordynamics

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## Outline of This Lecture

- Introduction
- Vibration related background
- Engineering vibration applications
- A first look on vibration analysis
- Vibration testing and control

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## Part I: Vibration: Brief Introduction

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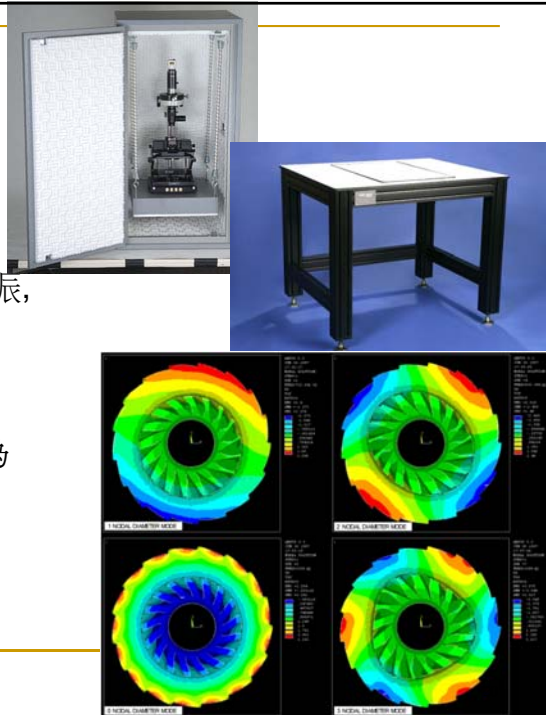
## Theory of Vibration

- Study the science, mathematics, and engineering of objects with oscillatory motion and the force associated with them
- Oscillatory motion
  - Any motion that repeats itself after an interval of time
  - Vibration frequency, vibration amplitude,...

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## 振動學應用範圍

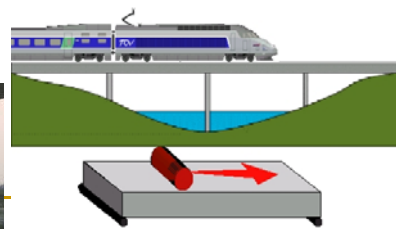
- 消除振動
  - 機械消音, 機械減振,
- 維持振動
  - 震盪器電路設計
- 鑑別系統動態行為
  - 模態分析



## 振動相關問題

- 地震與抗震
- 精密機械之定位
- 噪音與消音
- 振盪電路
- 汽車懸吊
- 衝擊

- ◆ 渦輪引擎之旋轉振動
- ◆ 橋樑/高速鐵路振動
- ◆ 中華一號衛星共振問題
- ◆ 流體誘發振動
- ◆ 材料疲勞與結構穩定
- ◆ 模態分析



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## Delta II Rocket



Payload

22

## 晉陞探空火箭「飛鼠一號」



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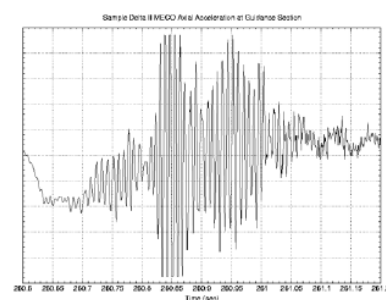
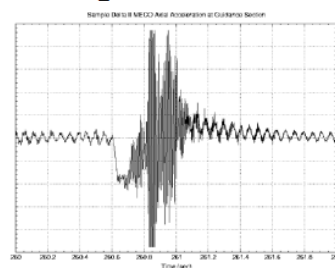


Main engine cut off

Mechanical Systems Analysis Branch/Code 542  
Goddard Space Flight Center

### MECO Transient Description

- Approximately 4g's input at 115 Hz - 125 Hz
- Short duration transient event lasting about 0.2 secs
- Event seen on all previous Delta II flights
- Higher magnitude and longer duration with newer main engines - Approximately 8 flights
- No known launch anomalies associated with event
- Is this event a driver for payload design???



## Part II: Vibration Related Courses / Books

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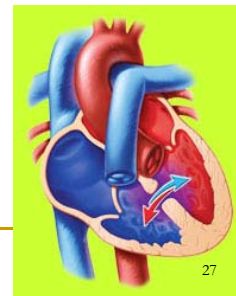
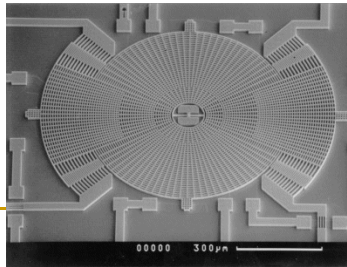
## 振動相關進階應用課程

- 結構動力學 (structural dynamics)
- 系統動態分析與控制器設計 (system dynamics analysis)
- 旋轉體動力學 (rotor dynamics)
- 微機電系統 (MEMS design)
- 非線性動力與混沌系統 (nonlinear vibration)
- 隨機振動 (random vibration)

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## 振動相關進階應用課程

- 聲學 (Acoustics)
- 空氣彈性力學 (Aeroelasticity)
- 結構控制 (structural control)
- Intelligent materials and structures



## 振動學所需基礎

- 牛頓力學
  - 應用力學 (II)
- 工程數學
  - 常微分方程 (Ordinary Differential Equations)
  - 線性代數 (Linear Algebra)
  - 富利葉分析 (Fourier Analysis)
  - 偏微分方程 (Partial Differential Equations)
  - 數值分析 (Numerical analysis)

## Part III: Vibration in Engineering Applications

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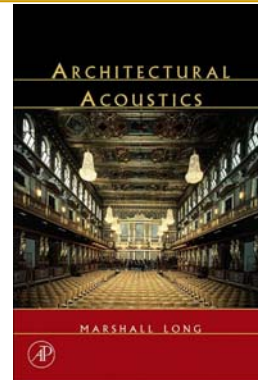
## 振動力學應用範圍: 機械領域

- 機械設計
  - machine element design
  - structural dynamic analysis
  - High speed rails
- 航空工程
  - Aeroelasticity , rotor dynamics
- 生物力學
  - Structure-fluid interaction
  - Hemodynamics

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## 振動力學應用範圍: 機械領域

- 聲學相關應用
  - Noise control of optical storage devices
  - Speaker and microphone design
- Diagnostics
  - Failure analysis
  - Fatigue



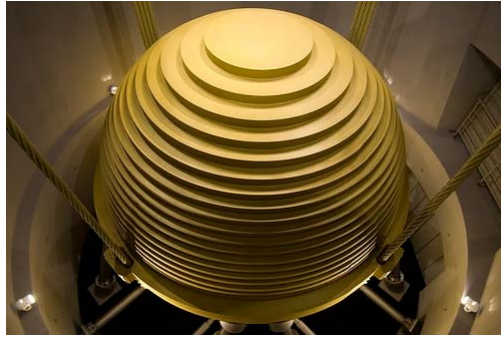
## 振動力學應用範圍: 電機領域

- 維持振動
  - Oscillator / resonator design
- 音響, 樂器, 揚聲器設計
  - Musical instrumentation with right resonant frequency and high Q



## 振動力學應用範圍: 土木領域

- 結構工程
  - Structural dynamics of buildings and bridges
- 地震工程
  - Earthquake engineering



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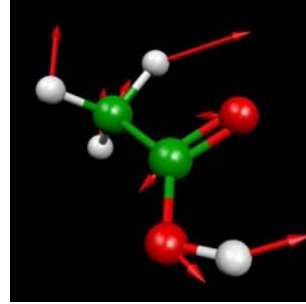
## 振動力學應用範圍: 系統與控制領域

- 系統建模
  - modeling of dynamic systems
- 結構控制
  - Active control of flexible systems
- 隨機系統
  - Random vibration

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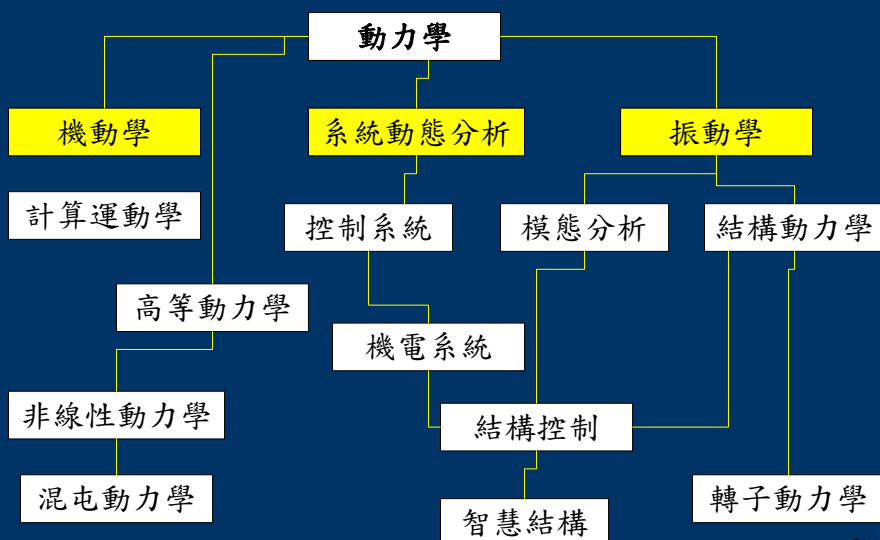
## 振動力學應用範圍: 微奈米領域

- 晶格振動
  - phonon
- 分子光譜
  - IR spectrum
- 感測器設計
  - Gyroscope
  - Accelerometers
  - Mass/ chemical sensors



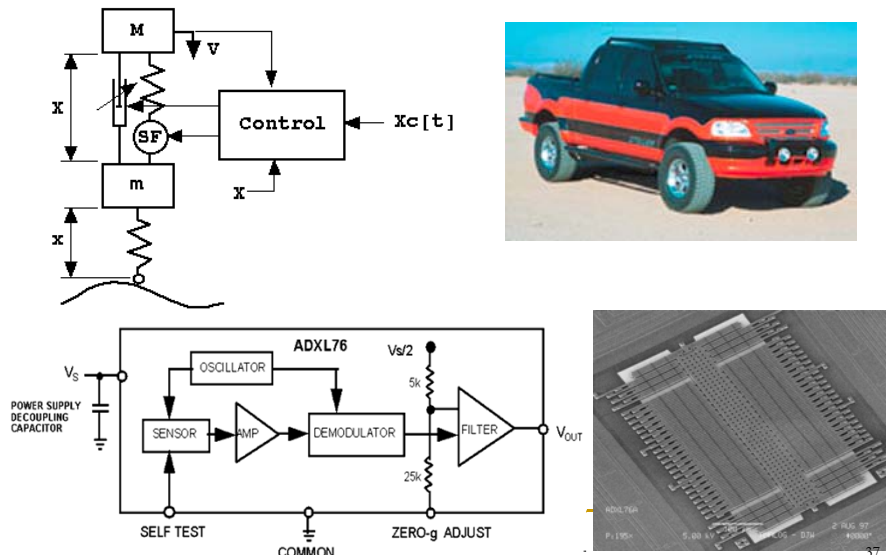
35

## 動力學後續相關領域介紹

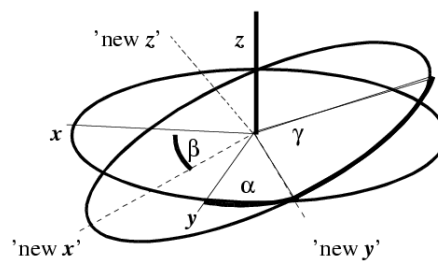
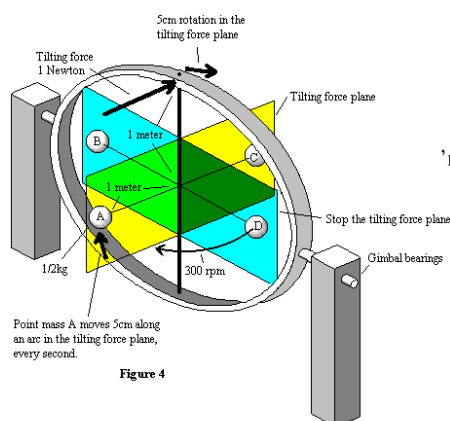


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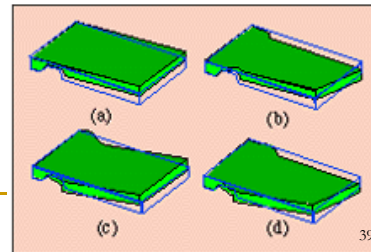
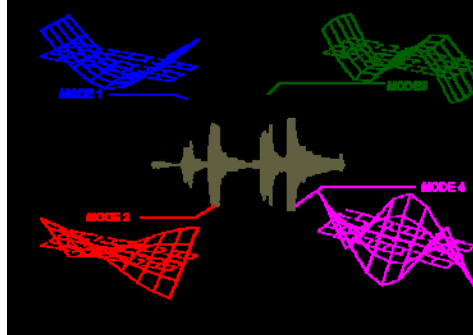
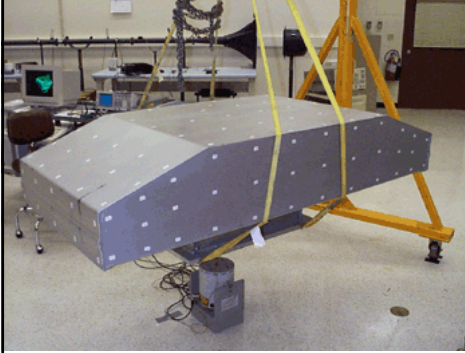
## 系統動態分析



# 高等動力學

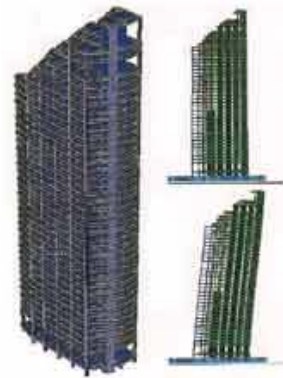
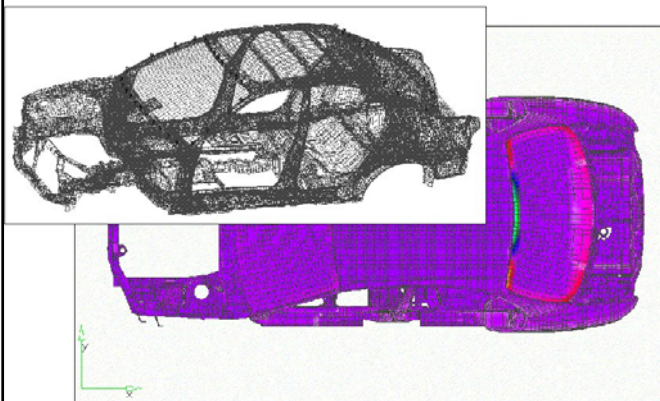


## 模態分析 (Modal Analysis)



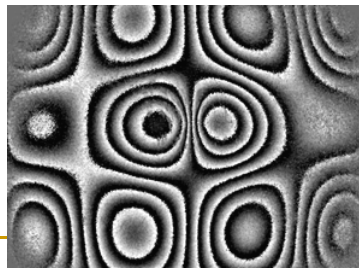
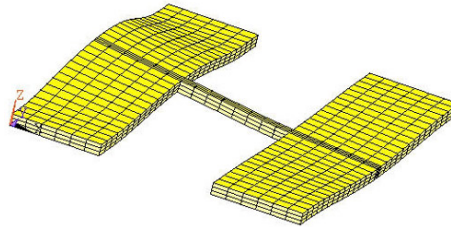
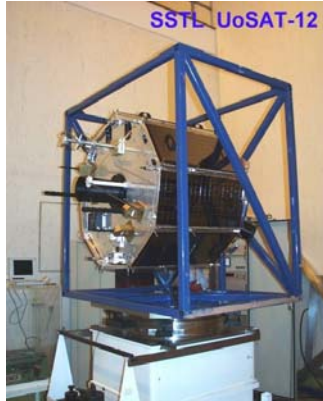
39

## 結構動力學 (Structural Dynamics)



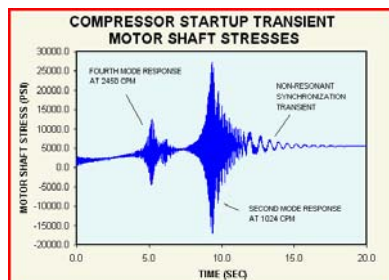
40

## 結構動力學 (Structural Dynamics)

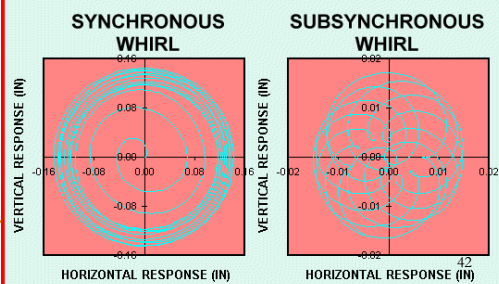


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## 轉子動力學 (Rotordynamics)

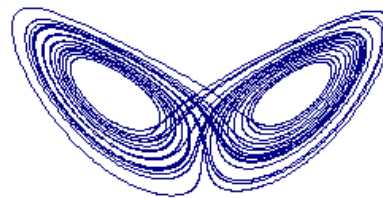
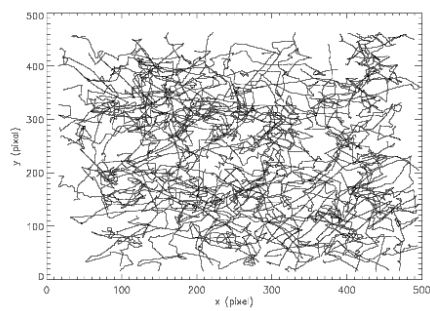
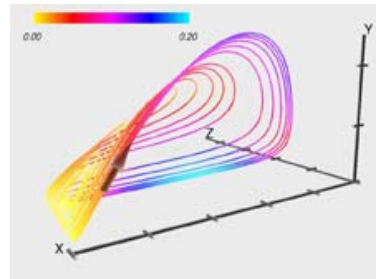
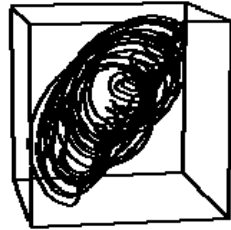


### TRANSIENT STARTUP ORBITS WITH AND WITHOUT SUBSYNCHRONOUS WHIRL



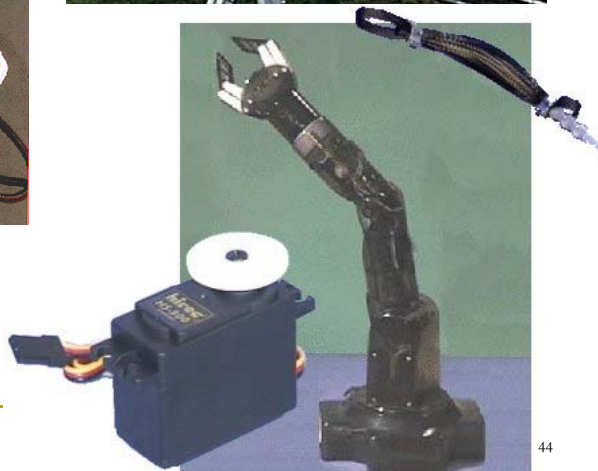
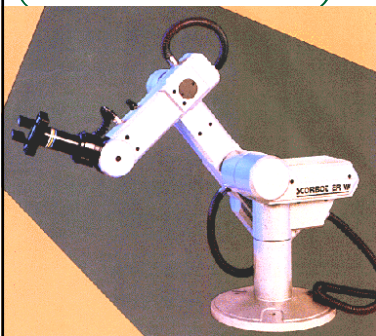


## 非線性動力學 (Nonlinear Dynamics)



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## 機電系統 (Mechatronics)



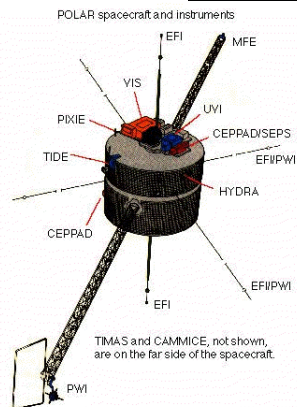
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## 太空動力學 (Space Dynamics)



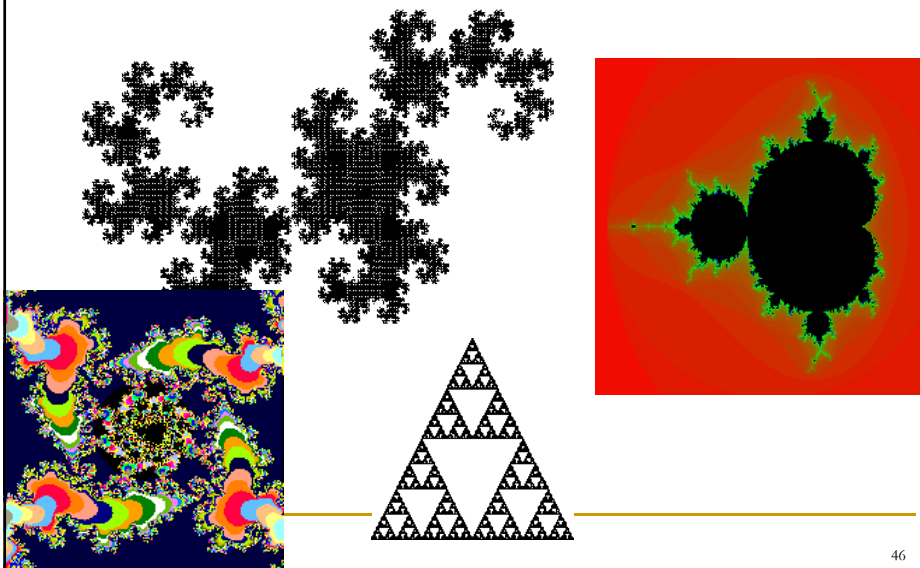
A goodbye Salute to Mir,  
She served her country proudly,  
Mir was truly a record-breaking  
achievement of human ingenuity.  
Thanks for letting us track your location  
for the millions of visitors to

**Liftoff to Space Exploration.**  
<http://liftoff.msfc.nasa.gov/>



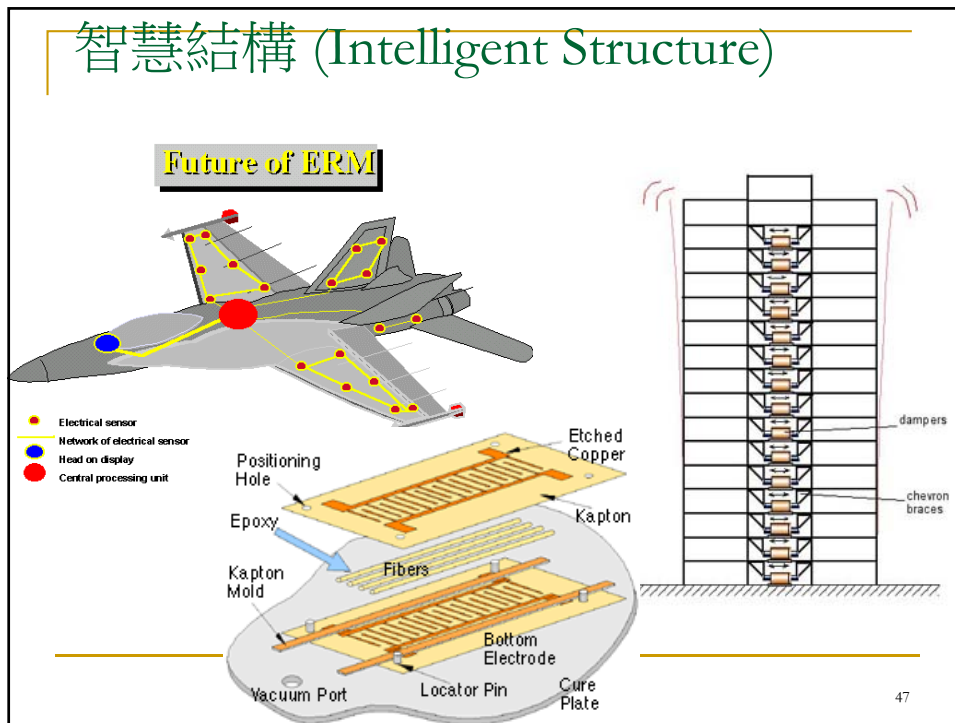
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## 混沌動力學 (Chaotic Dynamics; Dynamical Systems)

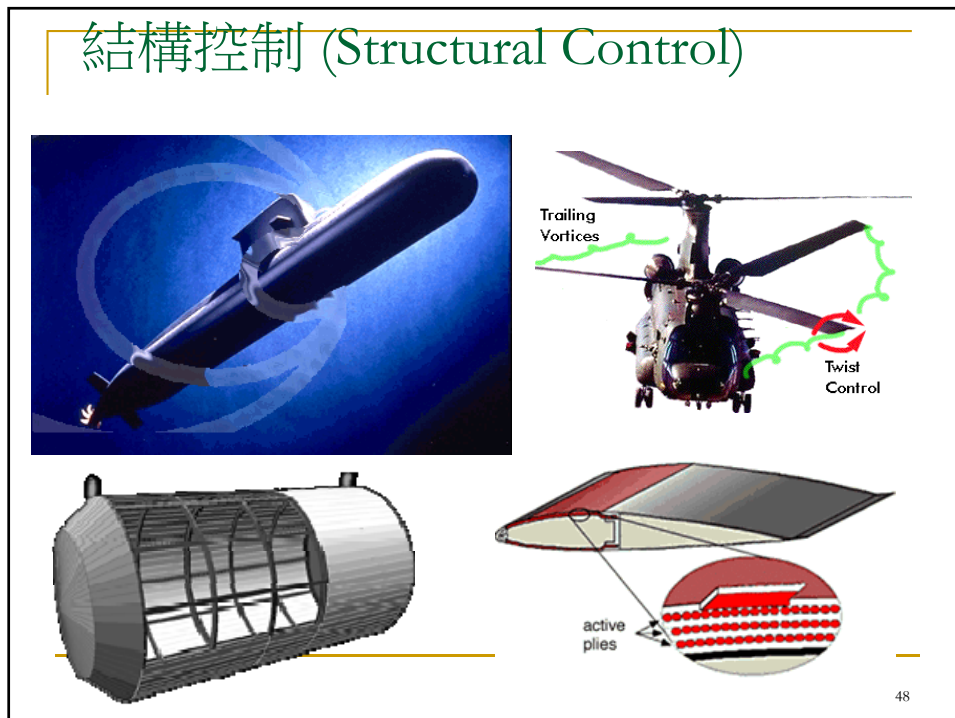


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## 智慧結構 (Intelligent Structure)



## 結構控制 (Structural Control)





## Tall Building

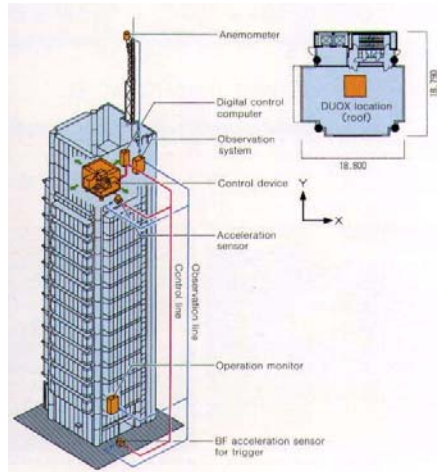
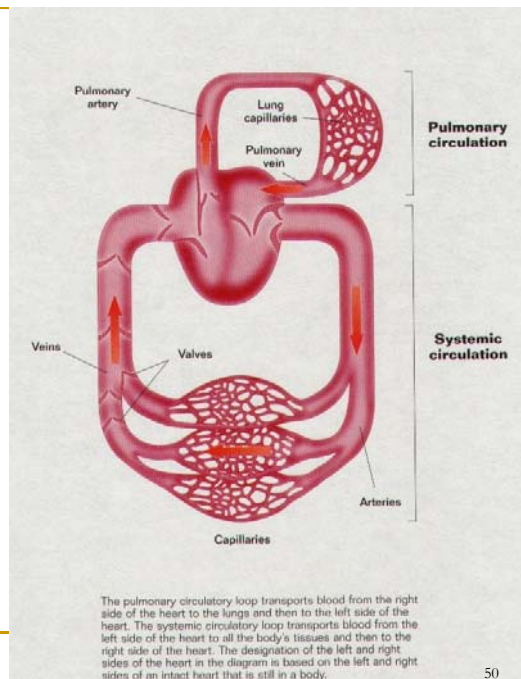
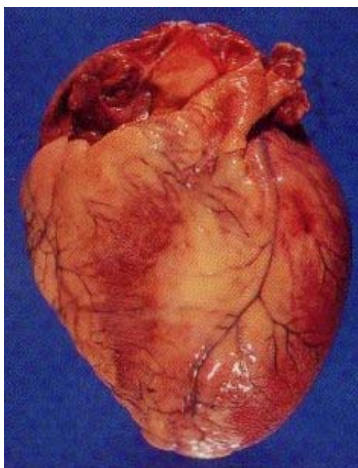


photo by Yehudi



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## Biomechanics Example



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## Biomechanics Example

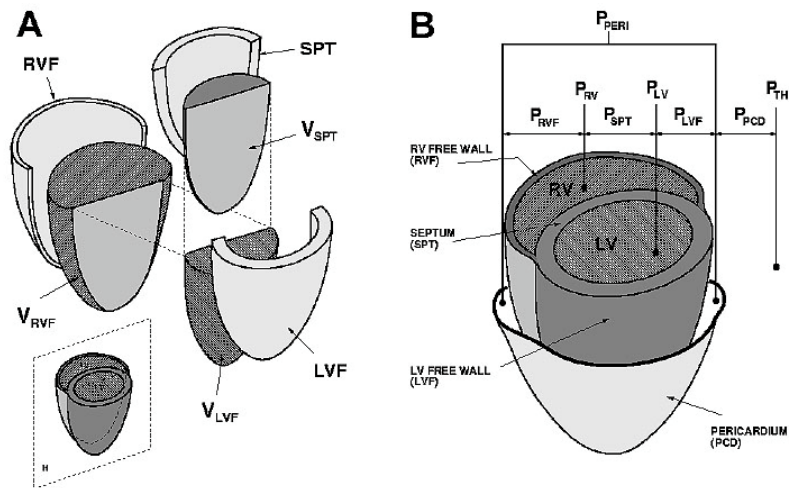


FIG. 1. Components of ventricular model: (A) volume distribution within the ventricles; (B) Force balance for coupled ventricles within pericardium. Source: Chung *et al.* (6).

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## Biomechanics Example

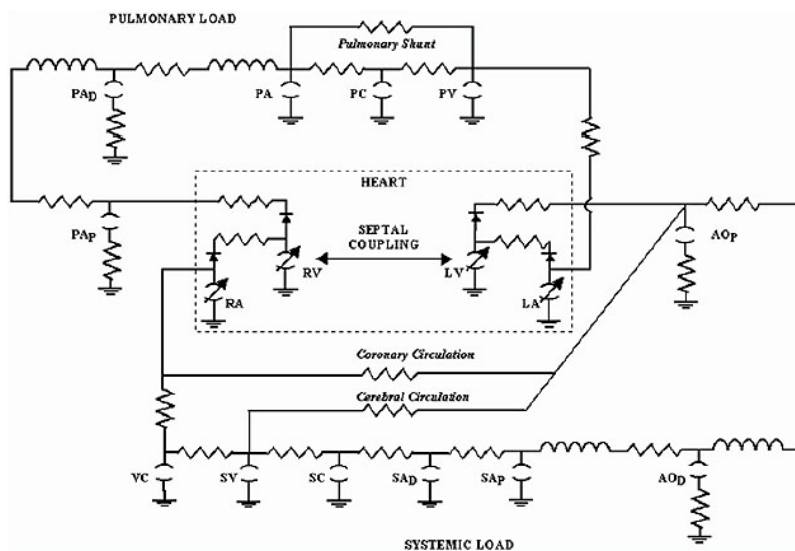
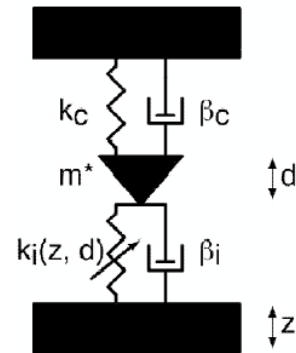
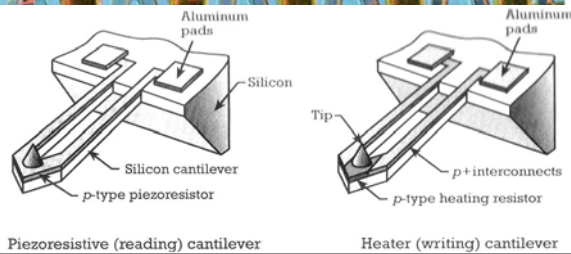
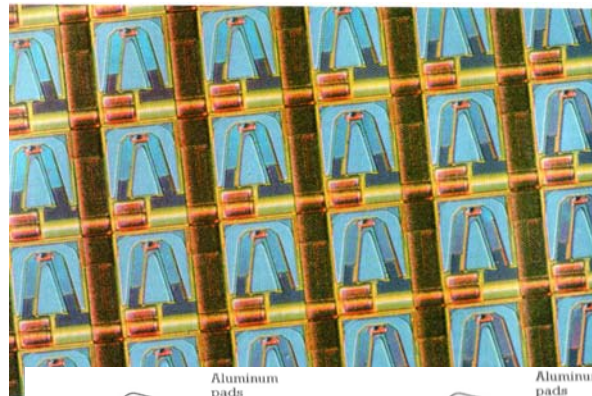


FIG. 3. Hydraulic equivalent schematic representation of the closed-loop circulatory model. Model parameters are listed in Table 1 and Appendix B.

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## AFM/SPM Example



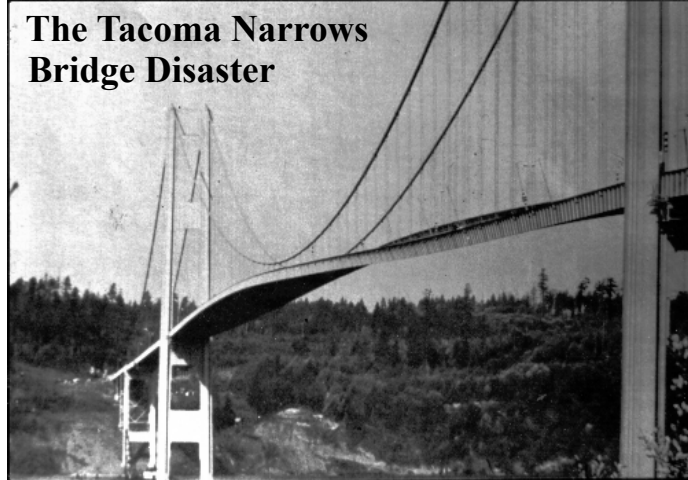
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## Part IV: A Quick Scan on Mechanical Vibration

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## Example: Flow induced vibration

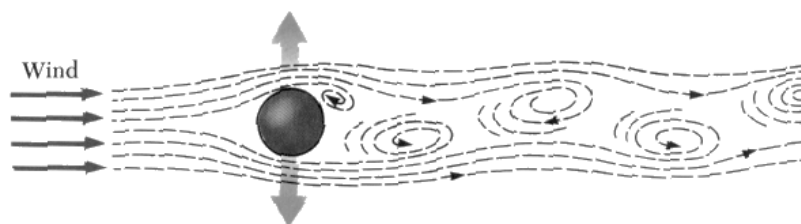
### The Tacoma Narrows Bridge Disaster



November 7, 1940

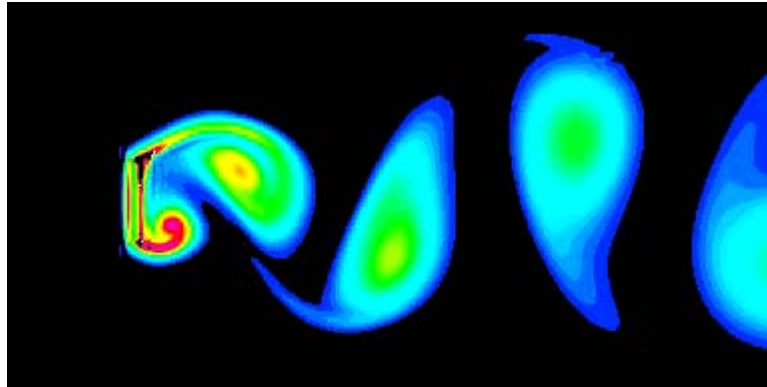


## Vortex Shedding



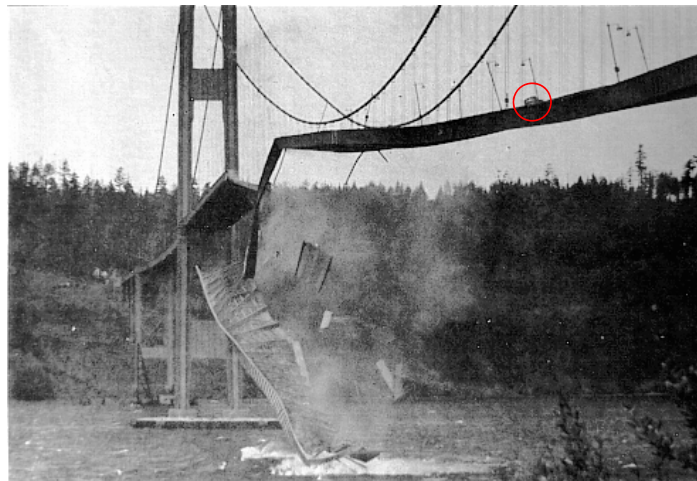
...Caused Wind-Induced Vibration

## Vortex Shedding



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## Tacoma Narrows Bridge



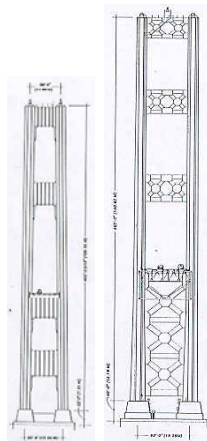
11:02 A.M. 600-ft span breaks away...

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## Part IV. A First Look on Vibration Analysis

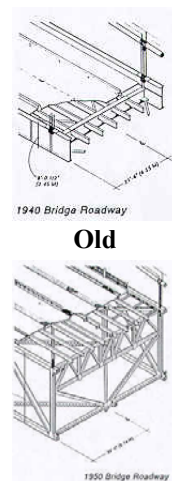
59

## Today's Tacoma Narrows Bridge



Old

New



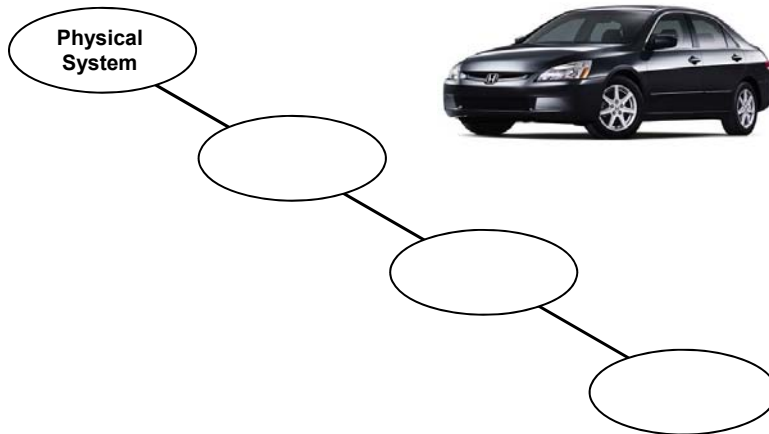
Old

New

60

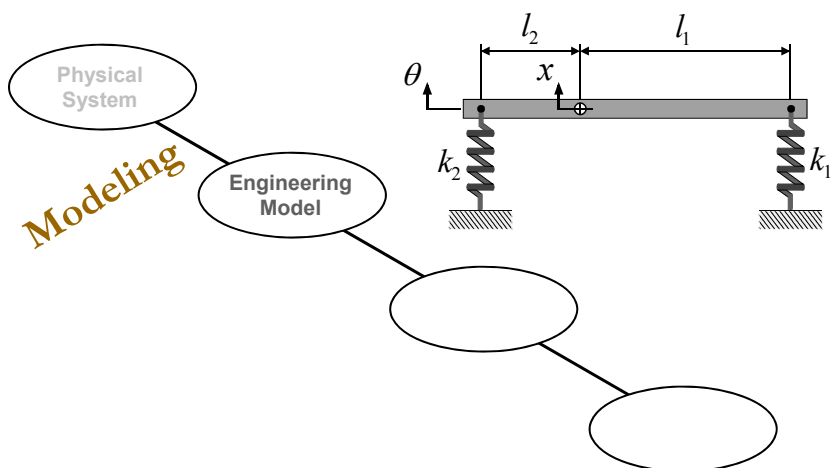


## Analyzing Vibration



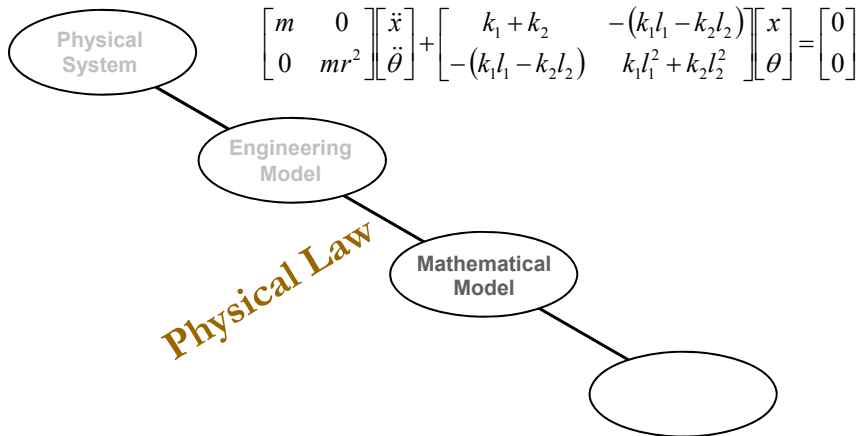
61

## Analyzing Vibration



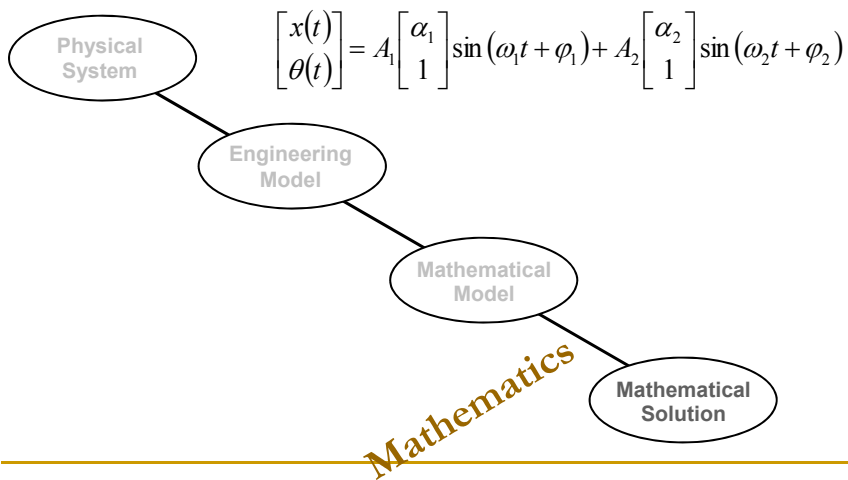
62

## Analyzing Vibration



63

## Analyzing Vibration

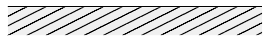


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## Modeling Vibration

### The Ingredients:



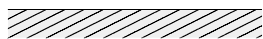
65

## Modeling Vibration

### The Ingredients:

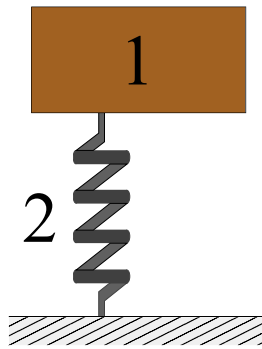


1. Inertia (stores kinetic energy)



66

## Modeling Vibration

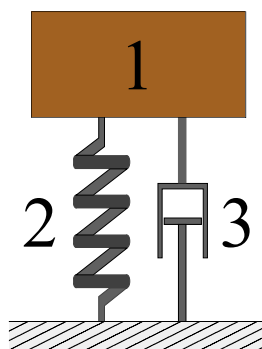


### The Ingredients:

1. Inertia (stores kinetic energy)
2. Elasticity (stores potential energy)

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## Modeling Vibration



### The Ingredients:

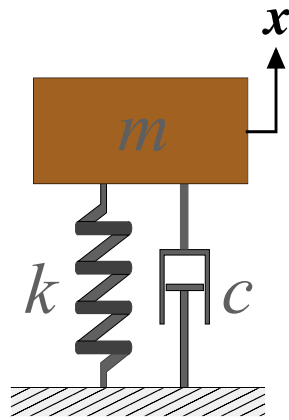
1. Inertia (stores kinetic energy)
2. Elasticity (stores potential energy)

### Realistic Addition:

3. Energy Dissipation

68

## Modeling Vibration



### The Ingredients:

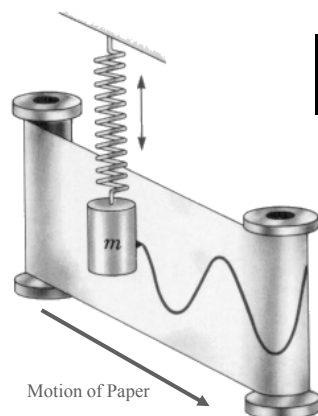
1. Mass,  $m$
2. Stiffness,  $k$

### Realistic Addition:

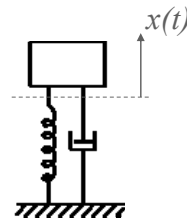
3. Damping,  $c$

69

## Simple Harmonic Motion

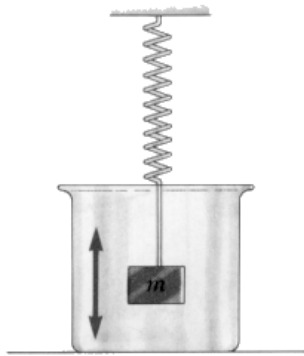


$$x(t) = A \sin(\omega_n t + \phi)$$



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## Simple Harmonic Motion with Damping

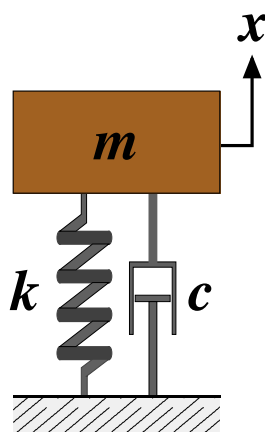


- Energy is converted to heat, sound, etc.

$$x(t) = Ae^{-\frac{t}{\tau}} \sin(\omega_n t + \phi)$$

71

## How is this model useful?



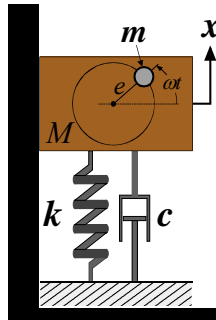
Can be used to model  
a:

- Motor vehicle
- Water tower
- Floating object

...and lots more!

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## Forced Vibration

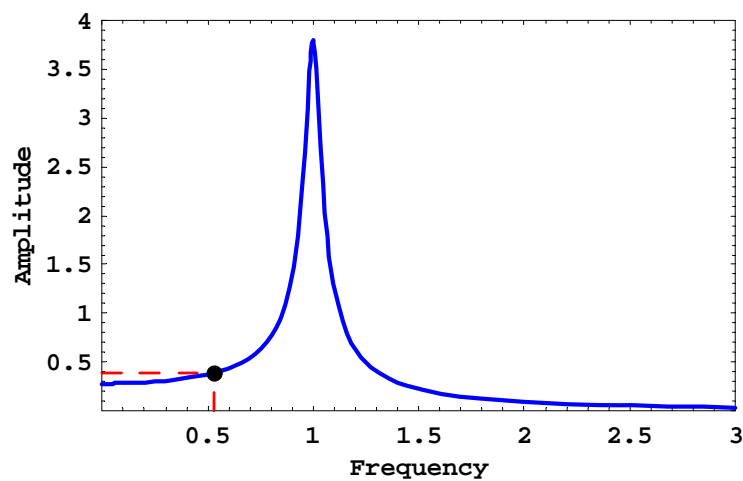


Steady-state Response:

$$x(t) = \frac{me\omega^2}{\sqrt{(k - M\omega^2)^2 + (c\omega)^2}} \sin(\omega t - \phi)$$

73

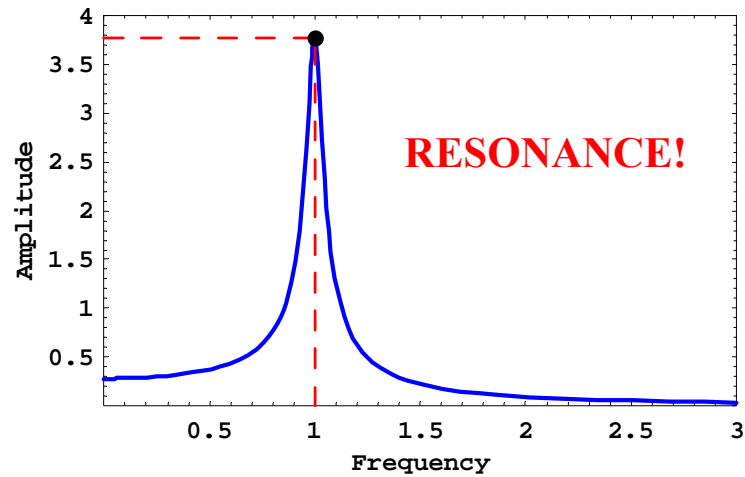
## Forced Vibration



Low Frequency  $\Rightarrow$  Small Amplitude

74

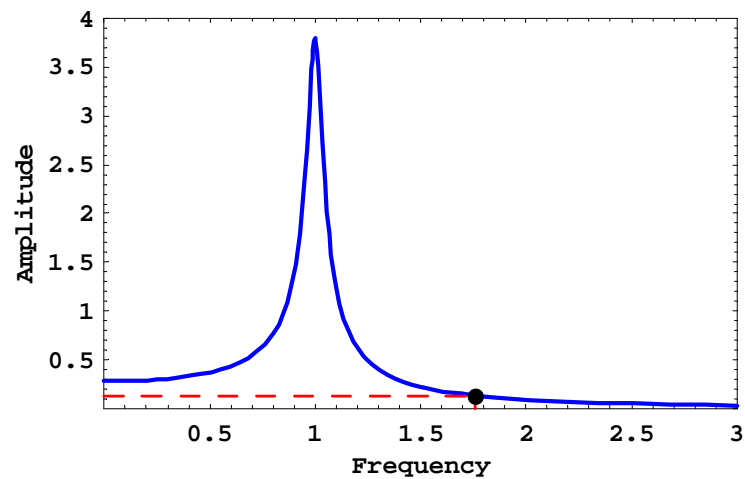
## Forced Vibration



Resonant Frequency  $\Rightarrow$  **Large Amplitude**

75

## Forced Vibration



Large Frequency  $\Rightarrow$  Small Amplitude

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## Mode Shapes

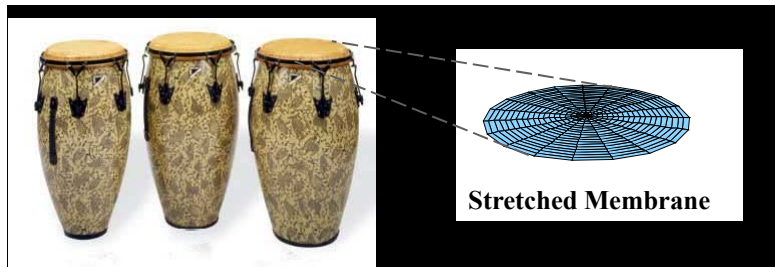
“Characteristic Geometry” of Vibration

77

## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 1:**



**Bongo Drums**

78

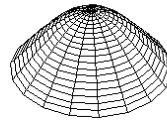
## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 1:**



**Bongo Drums**



**Mode 1**

79

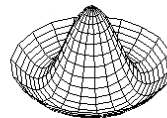
## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 1:**



**Bongo Drums**



**Mode 2**

80



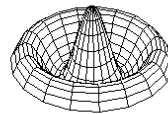
## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 1:**



**Bongo Drums**



**Mode 3**

81

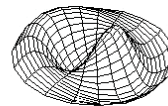
## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 1:**



**Bongo Drums**



**More complex modes...**

82

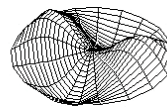
## Mode Shapes

“Characteristic Geometry” of Vibration

### EXAMPLE 1:



**Bongo Drums**



**More complex modes...**

83

## Mode Shapes

“Characteristic Geometry” of Vibration

### EXAMPLE 2:



**Acoustic Guitar**

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## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 2:**



**Acoustic Guitar**

**Mode 1**

85

## Mode Shapes

“Characteristic Geometry” of Vibration

**EXAMPLE 2:**



**Acoustic Guitar**

**Mode 2**

86

## Mode Shapes

“Characteristic Geometry” of Vibration

### EXAMPLE 2:



Acoustic Guitar

Mode 3

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## Mode Shapes

“Characteristic Geometry” of Vibration

### EXAMPLE 2:



Acoustic Guitar

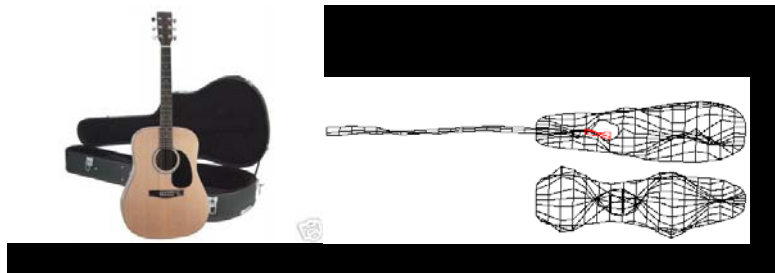
More complex modes...

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## Mode Shapes

“Characteristic Geometry” of Vibration

### EXAMPLE 2:



Acoustic Guitar

More complex modes...

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## Part V: Vibration Testing and Control

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## Modal Testing and Analysis

- Natural frequencies
- Mode shapes
- And their related applications
  - Material properties
  - NDT

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## 振動學實驗儀器簡介



加速規



衝擊錘

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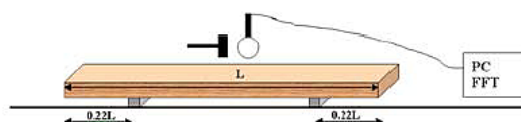
## 振動學實驗儀器簡介

### ■ 激振器 (shaker)

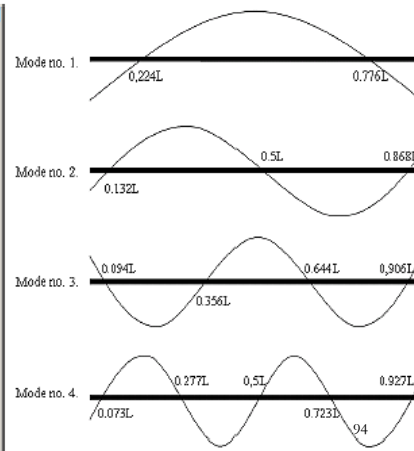
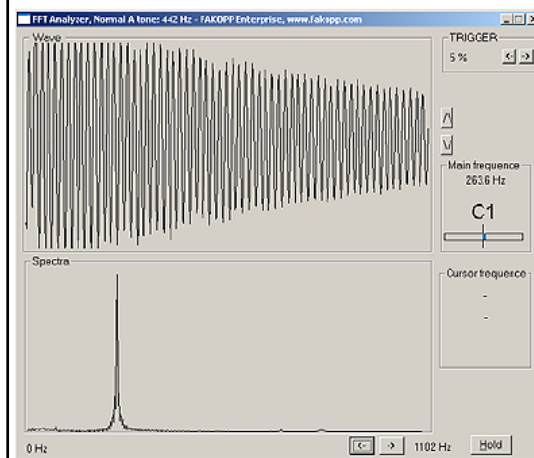


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## Dynamic MOE determination by bending vibration



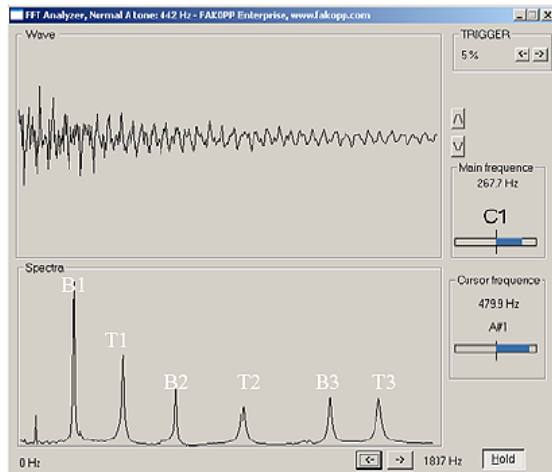
$$MOE_{dyn,bending} = \left( \frac{f_n}{C_n} \right)^2 \frac{mL^3}{I}$$



## Determination of shear modulus by torsion vibration

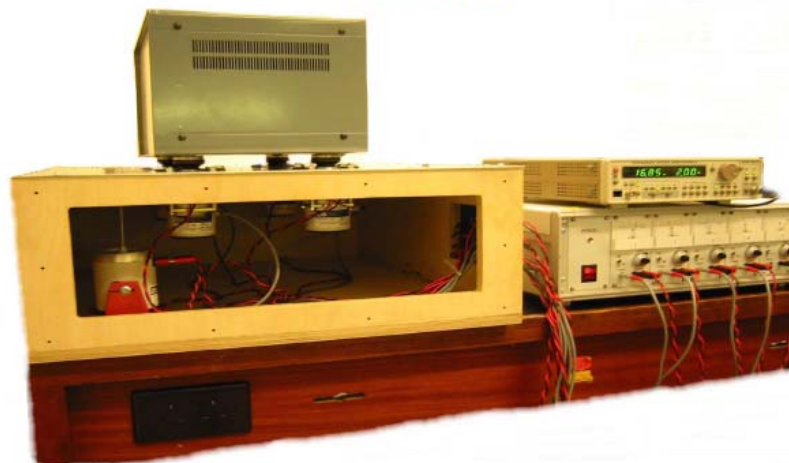


$$G_{dyn,torsion} = \left( \frac{2Lf_n}{n} \right)^2 \frac{\rho I_p}{K_t}$$



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## Laboratory demonstration of active vibration isolation



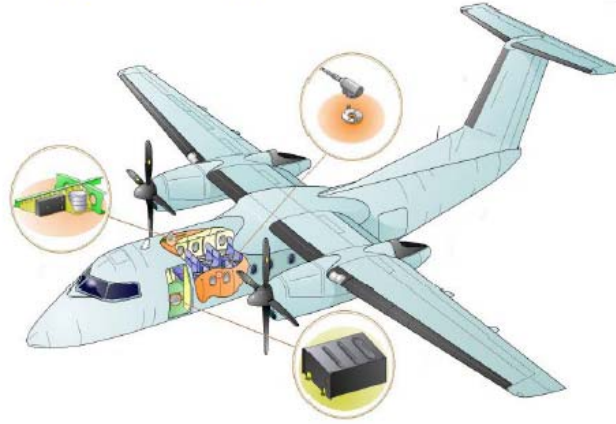
isvr

 University  
of Southampton

96



### Control System for Propeller Aircraft Active Noise System



Centralised digital system made by Ultra Electronics controls 5 harmonics with 48 structural actuators at 72 acoustic sensors, distributed throughout cabin.